

# ***REAL OPTIONS***

**Lecturer:** Prof. Marc CHESNEY, UNIZH

**First lecture:** June 11, 2009

**Location:** USI LUGANO

**Time:** Thu. June 11, 10:30 – 13:15 and 14:15 – 17:30, Fr. June 12, 9:00 -12:00 and 13:15 – 16:15.

Thu. June 18, 10:30 – 13:15 and 14:15 – 17:30, Fr. June 19, 9:15 -12:15 and 13:30 – 16:30 pm

**Language:** English

**Course duration:** 24 hours.

**Grades:** The final grades will be based on an oral or a written examination.

## **Contents:**

- The Limitations of the Traditional Net Present Value (NPV) Approach
- Dynamic Optimization under Uncertainty
- Real Options: the Basic Models of the Monopolistic Firm
- Lévy Processes and American Option Pricing: Applications to Real Options
- Real Options and Exotic Options
- Real Options and Competition
- Irreversible Investment Decisions in Presence of Incomplete Information
- Real Options and Environmental Finance

## **Description of the course:**

Investment (and disinvestment) decisions, which are crucial for economic growth, have a few essential characteristics: they are partially or totally irreversible, can be possibly delayed and are made in a risky environment. Taking these characteristics into consideration generates incentives to wait for better information before investing. More generally, it yields investment rules which are radically different from those corresponding to the standard Net Present Value (NPV) approach. The latter approach does not meet requirements, as it ignores the flexibility inherent in decision-making processes and the dynamic aspects of project selection.

The course aims firstly at explaining the basic real options models, after which more recent models will be presented. These include the introduction of competition and incomplete information into the real options framework. The use of the Real Options approach in Environmental Finance will also be presented. Finally, a particular focus on Lévy processes will be given. As the introduction of possible discontinuities is essential in some models, a clear understanding of Poisson processes is important. A standard background in stochastic calculus is required.

## Literature:

### BOOKS

1. BERTOIN J.  
**Lévy Processes**  
Cambridge University press, 2005.
2. CONT R. and P. TANKOV  
**Financial Modelling with Jump Processes**  
Chapman & Hall, 2004.
3. DIXIT A. and R. PINDYCK  
**Investment under Uncertainty**  
Princeton University Press, 1994.
4. ELLIOTT R. and E. KOPP  
**Mathematics of Financial Markets**  
Springer Finance, 2004.
5. FUDENBERG D. and J. TIROLE  
**Game Theory**  
The MIT Press, 1991.
6. HULL J.  
**Options, Futures and Other Derivative Securities**  
Prentice Hall, 2000.
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**Mathematical Methods for Financial Markets**  
Forthcoming Springer Verlag.
8. KARATZAS I. and S. SHREVE  
**Brownian Motion and Stochastic Calculus**  
Springer Verlag, 1988.
9. LAMBERTON D. and B. LAPEYRE  
**Introduction to Stochastic Calculus Applied to Finance,**  
Chapman & Hall, London, 1996.
10. REVUZ D. and M. YOR  
**Continuous Martingale and Brownian Motion**  
Springer Verlag, third edition, 1999.
11. ROSSETTO S.  
**Optimal Timing of Strategic Financial Decisions**  
Research Series, University of Amsterdam, 2002.
12. SCHWARTZ E. and L. TRIGEORGIS.  
**Real options and Investment under Uncertainty**  
**Classical Readings and recent Contributions**  
The MIT Press, 2004.
12. SMIT H.  
**Growth Options and Strategy Analysis**  
Erasmus University Rotterdam, 1996.

13. SMIT H. and L. TRIGEORGIS  
**Strategic Investment: Real Options and Games**  
Princeton University Press, 2004.

14. TRIGEORGIS L.  
**Real Options**  
The MIT Press, 1998.

## ARTICLES

1. ABEL A. and J. EBERLY  
**A Unified Model of Investment under Uncertainty**  
*American Economic Review*, 84:1369-1384, 1984.
2. BARONE-ADESI G. and R. WHALEY  
**Efficient Analytic Approximation of American Option Values**  
*Journal of Finance*, 42:301-320, 1987.
3. BELLAMY N. and M. JEANBLANC  
**Incomplete Markets with Jumps**  
*Finance and Sto.*, 4:209-222, 1999.
4. BOTTERON P., M. CHESNEY and R. GIBSON  
**An Application of Exotic Options to Firms' Delocalisation Policies under Exchange Rate Risk**  
*Journal of International Financial Markets, Institutions and Money*, 13:451-479, 2003.
5. BOYER M., E. GRAVEL and P. LASSERRE  
**Real Options and Strategic Competition: a Survey**  
Working paper, CIRANO, Canada, 2004.
6. BRENNAN, M.J. and E.S. SCHWARTZ,  
**Evaluating Natural Resource Investments**, *The Journal of Business* 58, 2,135-157, 1985.
7. CARR P., R. JARROW and R. MYNENI  
**Alternative Characterization of American Put Options**  
*Mathematical Finance*, 2:87-105, 1992.
8. CARR P. and L. WU  
**Time-changed Lévy Processes and Option Pricing**  
*Journal of Financial Economics*, 17:113-141, 2004.
9. CHESNEY M., and L. GAUTHIER  
**American Parisian Options**  
*Finance and Stochastics*, 10-475-506, 2006
10. CHESNEY M., and M. JEANBLANC  
**Pricing American Currency Options in an Exponential Lévy Model**  
*Appl. Mathematical Finance*, 11 : 207 – 225, 2004

11. CHESNEY M., and L. TASCHINI  
**The Endogeneous Price Dynamics of Emission Allowances and an Application to CO2 Option Pricing**  
Working paper, University of Zurich, 2008
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**Entry and Exit Decisions Under Uncertainty**  
*Journal of Political Economy*, 620-638, 1989.
13. DURBIN J.  
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**On the Discounted Penalty at Ruin in a Jump-Diffusion and the Perpetual Put Option**  
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**Stochastic Convenience Yield and the Pricing of Oil Contingent Claims**  
*Journal of Finance*, 45: 959-976, 1990.
18. KONG J. and Y. K. KWOCK  
**Real options in strategic investment games between two asymmetric firms**  
*European Journal of Operational Research*, 181: 967-985, 2007.
19. LAMBRECHT B. and W. PERRAUDIN  
**Real Options and Preemption under Incomplete Information**  
*Journal of Economics Dynamics and Control*, 27:619-643, 2003.
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*Quarterly Journal of Economics*, 101:707-728, 1986.
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**Real options in an asymmetric duopoly: Who benefits from your competition,**  
*Journal of Economics and Management Strategy*, 15: 1–35, 2006
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**Optimal Stopping Free Boundary and American Option in a Jump Diffusion Model**  
*Applied Math. and optim.*, 35:145-164, 1997.
26. RICH D.R.  
**The Mathematical Foundations of Barrier Option-Pricing Theory**  
*Advances in Futures and Options Research*, 7:267-311,1994
27. ROCHE H.  
**The Optimal Value of Waiting to Invest**  
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28. VILLENEUVE S., H. LOUBERGE and M. CHESNEY  
**Long Term Risk Management of Nuclear Waste: a Contingent Claim Analysis**  
*Journal of Economics Dynamics and Control*, 27:157-180, 2002
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**Formules Quasi-explicites pour les Options Américaines dans un Modèle de Diffusion avec Sauts**  
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